TEXTURE MAPPING

Texture Mapping

- We have our Phong-shaded objects, or maybe a raytraced image. It still doesn't look real.
- A major problem is surface detail. Now What?
  - Add more polygons or primitives. (slow!)
  - Add detail with a texture!
Texture Mapping: An Example

Image: Jeremy Birn

The Basic Algorithm

- Must map a 2D image to a 3D model.
- Use texture coordinates.
  - 2D coordinates (s,t), maps to 2D texture location.
  - Usually (s,t) are over \([0,1]\)
- Each vertex in polygon gets a texture coordinate.
- Or if a parametric model, use the \((u,v)\) of the model.
- Use linear interpolation to associate texels to a pixel

Is it simple?

- Although the idea is simple---map an image to a surface---there are 3 or 4 coordinate systems involved

Coordinate Systems

- Parametric coordinates
  - May be used to model curves and surfaces
- Texture coordinates
  - Used to identify points in the image to be mapped
- Object or World Coordinates
  - Conceptually, where the mapping takes place
- Window Coordinates
  - Where the final image is really produced

Texture Mapping
Mapping Functions

- Basic problem is how to find the maps
- Consider mapping from texture coordinates to a point a surface
- Appear to need three functions
  \[ x = x(s,t) \]
  \[ y = y(s,t) \]
  \[ z = z(s,t) \]
- But we really want to go the other way

Backward Mapping

- We really want to go backwards
- Given a pixel, we want to know to which point on an object it corresponds
- Given a point on an object, we want to know to which point in the texture it corresponds
- Need a map of the form
  \[ s = s(x,y,z) \]
  \[ t = t(x,y,z) \]
- Such functions are difficult to find in general

How Do Pixels and Texels Relate?

- Magnification
  - One pixel covers only a small part of a texel
- Minification
  - One pixel covers all or part of many texels

When Do We Interpolate

- Mapping techniques are implemented at the end of the rendering pipeline
- Very efficient because few polygons make it past the clipper
- Perspective projection is a non-linear transformation.
  - It can make a big difference if we interpolate before or after.
  - For proper foreshortening we should interpolate before perspective projection.

Interpolation

- Linear Interpolation
  - Take the closest texel and use its RGB value for shading.
  - Has problems. Especially at a distance, (Moiré patterns)
  - Take the average of the closest pixels.
  - Bilinear uses the four closest points
  - Trilinear – two bilinear filters
  - Anistropic – Elliptical mask for filter, expensive

How Do We Create the Mapping?

- Will a square picture map onto a sphere without distortion?
- How do you map a texture onto a wall?
- How about a cow?
- How about a car?
Two-Part Mapping

- Map to intermediate 3D object first.
- Then map 3D object to the final model.
- Typical intermediate objects: Cylinder, Cube, Sphere.

Example: map to cylinder

Two-Part Mapping: Planar

- Pick a plane, say xy plane of size (w,h)
- \( f(p) = (px/w, py/h) \)

Two-Part Mapping: Cube

- Easy to use with simple orthographic projection
- Also used in environment maps

Two-Part Mapping: Cylindrical

maps rectangle in \( u,v \) space to cylinder
of radius \( r \) and height \( h \) in world coordinates

\[
\begin{align*}
x &= r \cos 2\pi u \\
y &= r \sin 2\pi u \\
z &= v/h \\
s &= u \\
t &= v
\end{align*}
\]

maps from texture space

Two-Part Mapping: Rectangular Cylindrical

in a similar manner to the cylinder but have to decide where to put the distortion

\[
\begin{align*}
x &= r \cos 2mu \\
y &= r \sin 2mu \cos 2nv \\
z &= r \sin 2mu \sin 2nv
\end{align*}
\]

Spheres are used in environmental maps

Two-Part Mapping: Spherical

- Typical intermediate objects: Cylinder, Cube, Sphere.

Example: map to cylinder

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Spheres are used in environmental maps
Mapping to Intermediate Object?

- We are just determining the texture coordinate.
- Use the normal from intermediate object.
- Use the normal from the object.
- Use the centroid of the object.

How do We Apply the Texture?

- Decal (replace).
- Modulate (multiply).
- Blend (interpolate).
- Wrap (repeat).
- No wrap (no repeat).

Aliasing

- Point sampling of the texture can lead to aliasing errors

Point samples in \( u,v \) (or \( x,y,z \)) space

Point samples in texture space

Antialiasing: Mipmapping

- Pre-calculate the texture at various resolutions (powers of 2). Use the appropriate map based on the size of the polygon on the screen.
- Fast and somewhat accurate.
- How much extra storage does it take?

Area Averaging

A better but slower option is to use area averaging

Note that preimage of pixel is curved
Multiple Maps

- Can fix stretching at poles by using two maps
- Blend between them

Texture Mapping: Not Just Color

- Can apply to any shading attribute
- Color
- Specular Highlights
- Reflections
- Diffuse Reflections
- Normals
- Refraction
- Transparency

Texture Mapping Issues

- Tiling textures can introduce seems
  - A tileable texture will fix this
- If use an image, will have built in lighting that doesn’t match screen
- The mapping causes distortions
- Suffers from level of detail (minification, magnification)

Objectives

- Introduce the OpenGL texture functions and options

Basic Strategy

Three steps to applying a texture
1. Specify the texture
   - read or generate image
   - assign to texture
   - enable texturing
2. Assign texture coordinates to vertices
   - Proper mapping function is left to application
3. Specify texture parameters
   - wrapping, filtering
Texture Mapping and the OpenGL Pipeline

- Images and geometry flow through separate pipelines that join during fragment processing.
  - “Complex” textures do not affect geometric complexity.

Define Image as a Texture

```c
glTexImage2D( target, level, components, 
w, h, border, format, type, texels );
```

- `target`: type of texture, e.g., `GL_TEXTURE_2D`
- `level`: used for mipmapming (discussed later)
- `components`: elements per texel
- `w, h`: width and height of `texels` in pixels
- `border`: used for smoothing (discussed later)
- `format` and `type`: describe `texels`
- `texels`: pointer to `texel` array

```c
glTexImage2D(GL_TEXTURE_2D, 0, 3, 512, 512, 0, 
GL_RGB, GL_UNSIGNED_BYTE, my_texels);
```

Mapping a Texture

- Based on parametric texture coordinates
- `glTexCoord*()` specified at each vertex
**Typical Code**

```cpp
offset = 0;
GLuint vPosition = glGetAttribLocation( program, "vPosition" );
glEnableVertexAttribArray( vPosition );
glVertexAttribPointer( vPosition, 4, GL_FLOAT, GL_FALSE, 0, BUFFER_OFFSET(offset) );
offset += sizeof(points);
GLuint vTexCoord = glGetAttribLocation( program, "vTexCoord" );
glEnableVertexAttribArray( vTexCoord );
glVertexAttribPointer( vTexCoord, 2, GL_FLOAT, GL_FALSE, 0, BUFFER_OFFSET(offset) );
```

**Interpolation**

OpenGL uses interpolation to find proper texels from specified texture coordinates. Interpolation can be distortions, depending on the good or poor selection of tex coordinates. For example, texture stretched over a trapezoid showing effects of bilinear interpolation.

**Texture Parameters**

- OpenGL has a variety of parameters that determine how texture is applied.
- Wrapping parameters determine what happens if s and t are outside the (0,1) range.
- Filter modes allow us to use area averaging instead of point samples.
- Mipmapping allows us to use textures at multiple resolutions.
- Environment parameters determine how texture mapping interacts with shading.

**Wrapping Mode**

Clamping: if \( s, t > 1 \) use 1, if \( s, t < 0 \) use 0.

Wrapping: use \( s, t \) modulo 1

- \( \text{glTexParameteri}( \text{GL_TEXTURE}_2D, \text{GL_TEXTURE_WRAP}_S, \text{GL_CLAMP} ) \)
- \( \text{glTexParameteri}( \text{GL_TEXTURE}_2D, \text{GL_TEXTURE_WRAP}_T, \text{GL_REPEAT} ) \)

**Filter Modes**

Modes determined by

- \( \text{glTexParameteri}( \text{target}, \text{type}, \text{mode} ) \)

- \( \text{glTexParameteri}( \text{GL_TEXTURE}_2D, \text{GL_TEXTURE_MAG_FILTER}, \text{GL_NEAREST} ) \)
- \( \text{glTexParameteri}( \text{GL_TEXTURE}_2D, \text{GL_TEXTURE_MIN_FILTER}, \text{GL_LINEAR} ) \)

Note that linear filtering requires a border of an extra texel for filtering at edges (border = 1).
Mipmapped Textures

- *Mipmapping* allows for prefiltered texture maps of decreasing resolutions
- Lessens interpolation errors for smaller textured objects
- Declare mipmap level during texture definition
  ```c
  glTexImage2D( GL_TEXTURE_*D, level, ... )
  ```

Example

![Point sampling](image1)

![Linear filtering](image2)

![Mipmapped point sampling](image3)

![Mipmapped linear filtering](image4)

Texture Functions

- Controls how texture is applied
  ```c
  glTexEnv{fi}v(GL_TEXTURE_ENV, prop, param)
  ```
- GL_TEXTURE_ENV_MODE modes
  - GL_MODULATE: modulates with computed shade
  - GL_BLEND: blends with an environmental color
  - GL_REPLACE: use only texture color
  - GL(GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE, GL_MODULATE);
- Set blend color with GL_TEXTURE_ENV_COLOR

Perspective Correction Hint

- Texture coordinate and color interpolation
  - either linearly in screen space
  - or using depth/perspective values (slower)
- Noticeable for polygons "on edge"
  ```c
  glHint(GL_PERSPECTIVE_CORRECTION_HINT, hint)
  ```
  where hint is one of
  - GL_DONT_CARE
  - GL_NICEST
  - GL_FASTEST

Generating Texture Coordinates

- OpenGL can generate texture coordinates automatically
  ```c
  glTexGen{ifd}v(GL_TEXTURE_ENV, GL_TEXTURE_ENV_MODE, GL_MODULATE);
  ```
- specify a plane
  - generate texture coordinates based upon distance from the plane
- generation modes
  - GL_OBJECT_LINEAR
  - GL_EYE_LINEAR
  - GL_SPHERE_MAP (used for environmental maps)

Texture Objects

- Texture is part of the OpenGL state
  - If we have different textures for different objects, OpenGL will be moving large amounts data from processor memory to texture memory
  - Recent versions of OpenGL have *texture objects*
    - one image per texture object
    - Texture memory can hold multiple texture objects
Applying Textures II
1. specify textures in texture objects
2. set texture filter
3. set texture function
4. set texture wrap mode
5. set optional perspective correction hint
6. bind texture object
7. enable texturing
8. supply texture coordinates for vertex
   • coordinates can also be generated

Other Texture Features
• Environment Maps
  • Start with image of environment through a wide angle lens
  • Can be either a real scanned image or an image created in OpenGL
  • Use this texture to generate a spherical map
  • Use automatic texture coordinate generation
• Multitexturing
  • Apply a sequence of textures through cascaded texture units